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SUPERVISOR'S USE ONLY

Level 2 Mathematics and Statistics, 2016

91262 Apply calculus methods in solving problems

9.30 a.m. Thursday 24 November 2016
Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply calculus methods in solving problems.	Apply calculus methods, using relational thinking, in solving problems.	Apply calculus methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Make sure that you have Formulae Sheet L2–MATHF.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

You must show the use of calculus in answering all questions in this paper.

Check that this booklet has pages 2–12 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

TOTAL

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QUESTION ONE

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- (a) A function f is given by $f(x) = 4x^3 - 7x^2 + 2x - 4$.

Find the gradient of the graph of the function at the point where $x = 2$.

- (b) The line $y = x + 3.25$ is a tangent to the graph of the function $f(x) = 3x^2 - 2x + 4$.

Use calculus to show that the line is a tangent to the curve, and that the point where this tangent touches the curve is $(0.5, 3.75)$.

- (c) The function $f(x) = 2x^3 + kx^2 + 5$ has a minimum turning point when $x = 1$.

What are the coordinates of the **maximum** turning point?

- (d) The equation of a function $y = f(x)$ has gradient function of the form $f'(x) = 2x - a$, where a is a constant.

The point (3,4) is the turning point on the graph of the function.

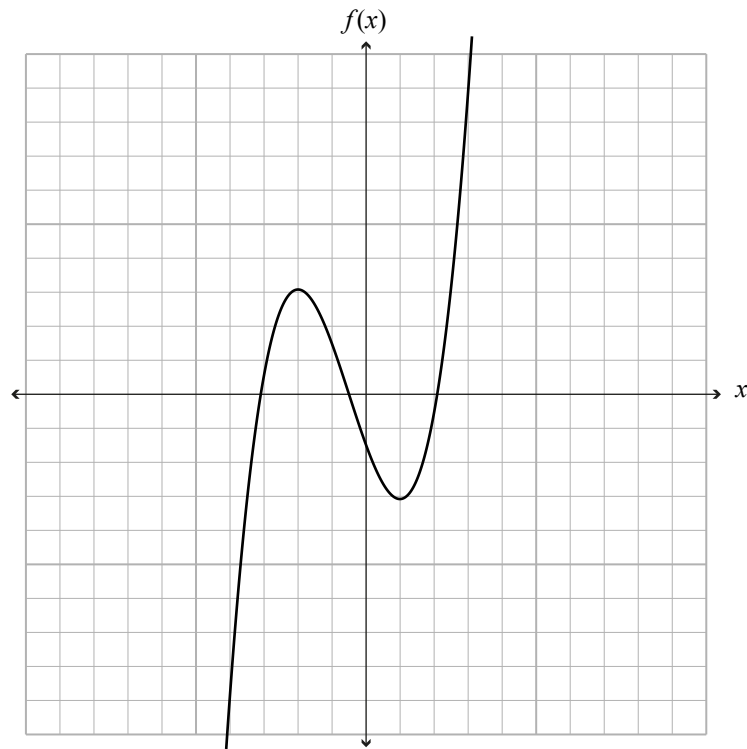
Find the equation of the function.

- (e) Find the local minimum value of the function $y = x^3(x - 4)$.

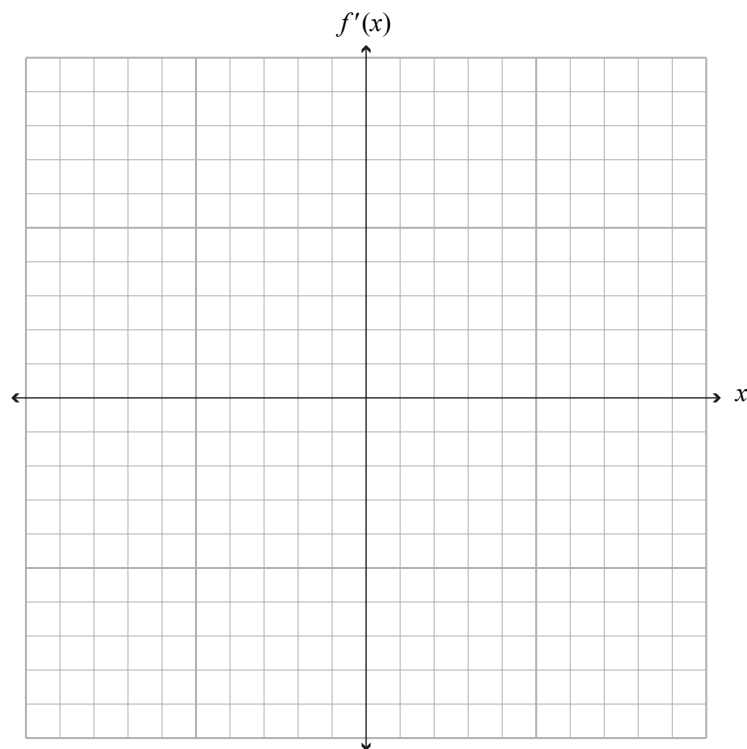
Justify your answer.

QUESTION TWO

- (a) The diagram below shows the graph of the function $y = f(x)$.



On the axes below sketch the gradient function $y = f'(x)$.



If you need to redraw this graph, use the grid on page 11.

This question has been corrected from that used in the examination.

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- (b) The line $y = ax + b$ is a tangent to the graph of the function $y = 2x^2 - 3x + 1$ at the point $(2,3)$.

Find the values of a and b .

- (c) A function f is given by $f(x) = 2 - 4x + 5x^2 + ax^3$.

The gradient of the graph of the function at the point where $x = 1$ is 3.

Find the value of a .

- (Area of circle = πr^2)

- Find the range of values of x in terms of a for which the function is decreasing.

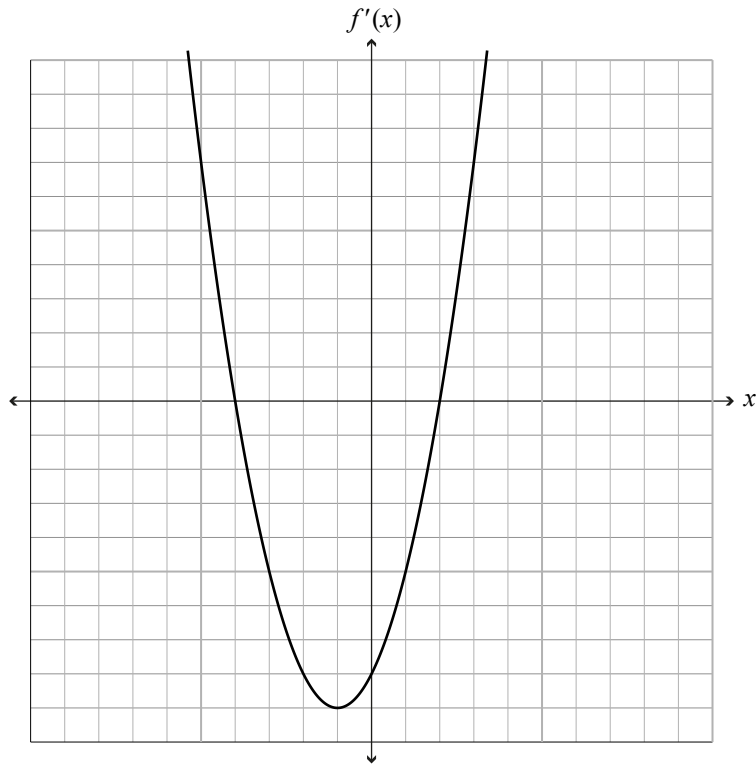
QUESTION THREEASSESSOR'S
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- (a) The gradient function for a curve is given by $\frac{dy}{dx} = 3x^2 - 5$.

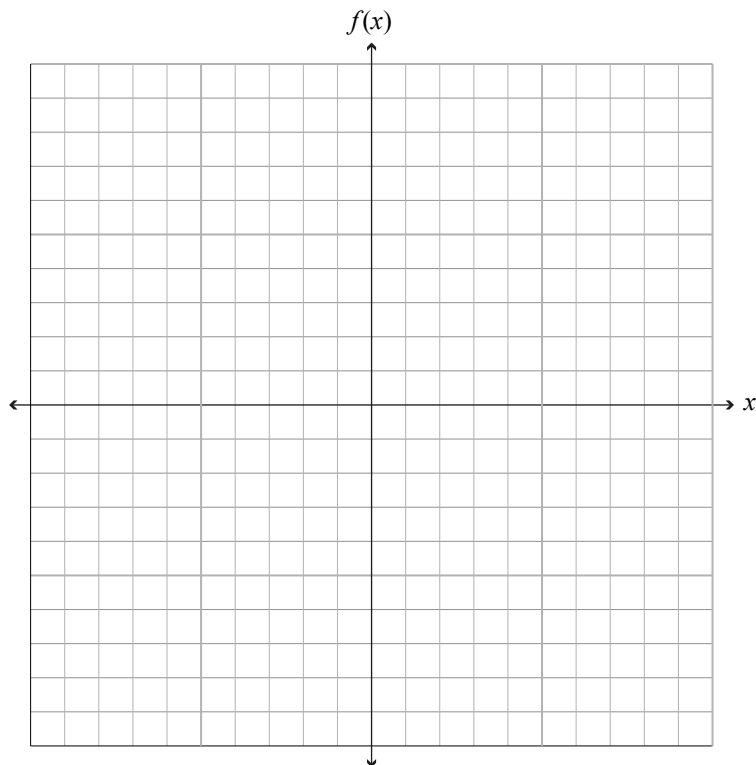
The curve passes through the point (1,0).

Find the equation of the curve.

- (b) The diagram below shows the graph of the gradient function $y = f'(x)$ of a function $y = f(x)$.



On the axes below sketch the graph of the function $y = f(x)$.



*If you need
to redraw this
graph, use the
grid on page 11.*

- (c) Meg is riding her motocross bike.

When she passes a fixed point P on the track, she has a speed, v , of 5 m s^{-1} , and her acceleration, a , is 0.6 m s^{-2} .

- (i) If she were to continue to accelerate at this rate, what is her speed when she has been riding for 10 seconds after passing P?

- (ii) How far will she have travelled from P when she reaches a speed of 8 m s^{-1} ?

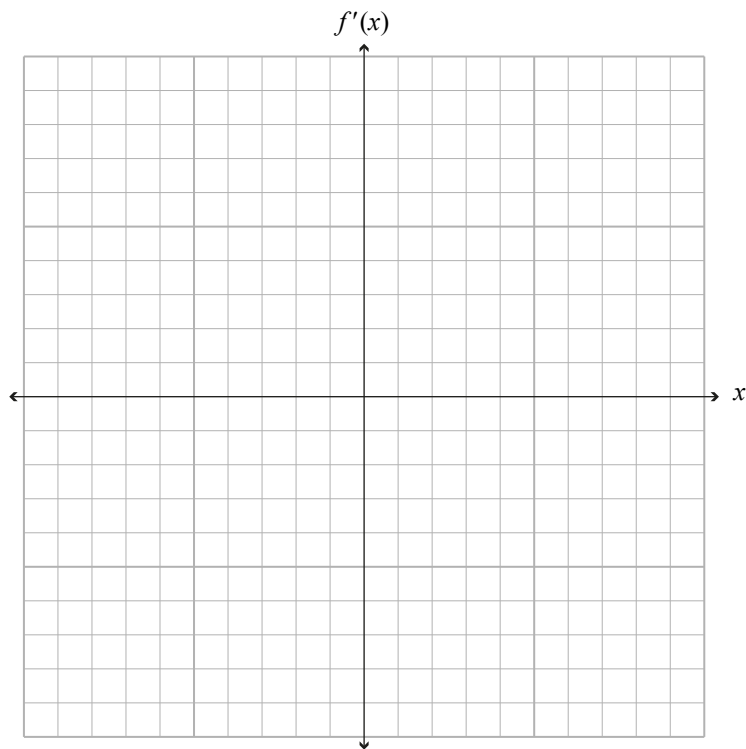
**Question Three continues
on the following page.**

- (iii) Meg's friend Leo was riding with her, but he begins to decelerate when they reach a speed of 8 m s^{-1} .

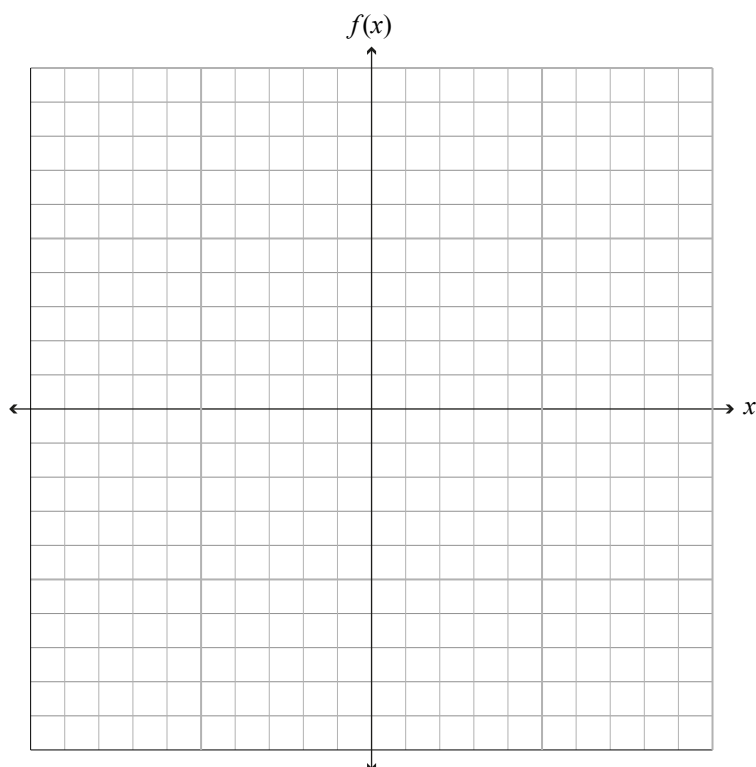
If he decelerates at 0.2 m s^{-2} , how far past the point P will he be when he reaches a speed of 6 m s^{-1} ?

SPARE GRIDSASSESSOR'S
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If you need to redraw your graph from Question Two (a), draw it on the grid below. Make sure it is clear which answer you want marked.



If you need to redraw your graph from Question Three (b), draw it on the grid below. Make sure it is clear which answer you want marked.



Extra paper if required.
Write the question number(s) if applicable.

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QUESTION
NUMBER

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